

Einführung in die Computerlinguistik

Text Classification and Naive Bayes

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Dieses Foliensatz wurde von Prof. Dr. Hinrich Schütze erstellt.

Fehler und Mängel sind ausschließlich meine Verantwortung.

Outline

- 1 Text classification
- 2 Naive Bayes
- 3 NB theory
- 4 Evaluation of TC

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A text classification task: Email spam filtering

From: '''' <takworldd@hotmail.com>

Subject: real estate is the only way... gem oalvgkay

Anyone can buy real estate with no money down

Stop paying rent TODAY !

There is no need to spend hundreds or even thousands for similar courses

I am 22 years old and I have already purchased 6 properties using the methods outlined in this truly INCREDIBLE ebook.

Change your life NOW !

=====
Click Below to order:

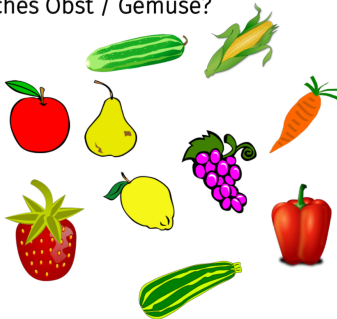
<http://www.wholesaledaily.com/sales/nmd.htm>

Mustererkennung (pattern recognition)



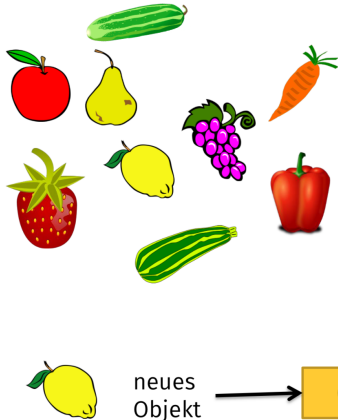
Kamera

Welches Obst / Gemüse?



Was sind mögliche
Erkennungsmerkmale?

Mustererkennung (pattern recognition)



Merkmale/Attribute:

- Farbe
- Größe
- Form
- ...

Beispiele:
Attribute/Werte + richtige Klasse

Algorithmus
(Maschinelles Lernen)

neues
Objekt → **Classifier**

→ Zitrone (80%)
Birne (20%)

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Using a learning method or **learning algorithm**, we then wish to learn a **classifier** γ that maps documents to classes:

$$\gamma : \mathbb{X} \rightarrow \mathbb{C}$$

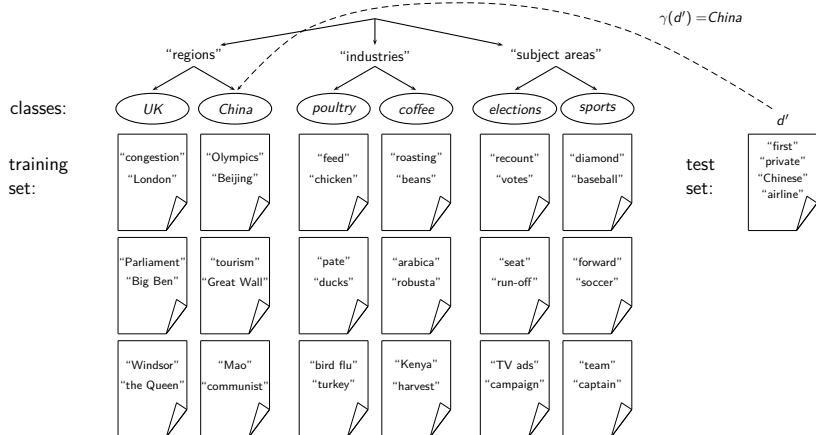
We can view sentences also as documents – so “document” refers to any piece of text we want to classify.

Formal definition of TC: Application/Testing

Given: a description $d \in \mathbb{X}$ of a document

Determine: $\gamma(d) \in \mathbb{C}$, that is,
determine the class that is most appropriate for d

Topic classification



Applications of text classification

- Language identification
(classes: English vs French vs ...)
- The automatic detection of spam pages
(spam vs nonspam)
- Sentiment analysis:
Is a movie or product review positive or negative
(positive vs negative)
- Topic-specific or *vertical* search:
Restrict search to a “vertical” like “related to health”
(classes: relevant to vertical vs not)

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- → We need automatic methods for classification.

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- Accuracy is very high if a rule has been carefully refined over time by a subject expert.
- Building and maintaining rule-based classification systems is cumbersome and expensive.

A Verity topic (a complex classification rule)

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```
comment line      # Beginning of art topic definition
top-level topic  art ACCRUE
                 /author = "fsmith"
topic definition modifiers {
                 /date  = "30-Dec-01"
                 /annotation = "Topic created
                             by fsmith"
subtopic topic    * 0.70 performing-arts ACCRUE
evidencetopic    ** 0.50 WORD
topic definition modifier /wordtext = ballet
evidencetopic    ** 0.50 STEM
topic definition modifier /wordtext = dance
evidencetopic    ** 0.50 WORD
topic definition modifier /wordtext = opera
evidencetopic    ** 0.30 WORD
topic definition modifier /wordtext = symphony
subtopic         * 0.70 visual-arts ACCRUE
                 ** 0.50 WORD
                 /wordtext = painting
                 ** 0.50 WORD
                 /wordtext = sculpture
subtopic         * 0.70 film ACCRUE
                 ** 0.50 STEM
                 /wordtext = film
subtopic         ** 0.50 motion-picture PHRASE
                 *** 1.00 WORD
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- No free lunch: requires hand-classified training data
- But this manual classification can be done by non-experts.

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- If a document's terms do not provide clear evidence for one class vs. another, we choose the c with highest $P(c)$.

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Find the “best” class
- The best class is the most likely or **maximum a posteriori (MAP) class** c_{map} :

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} \hat{P}(c|d) = \operatorname{argmax}_{c \in \mathbb{C}} \hat{P}(c) \prod_{1 \leq k \leq n_d} \hat{P}(t_k|c)$$

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- So what we usually compute in practice is:

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} [\log \hat{P}(c) + \sum_{1 \leq k \leq n_d} \log \hat{P}(t_k | c)]$$

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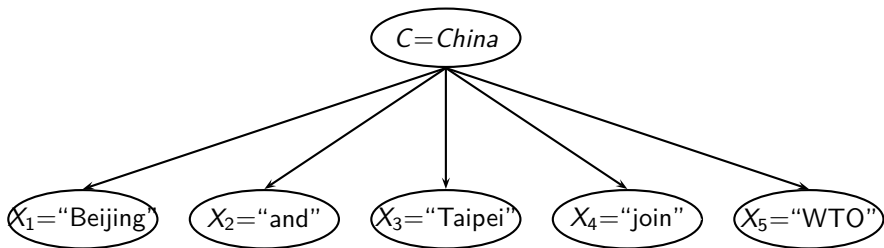
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- T_{ct} is the number of tokens of t in training documents from class c (includes multiple occurrences)

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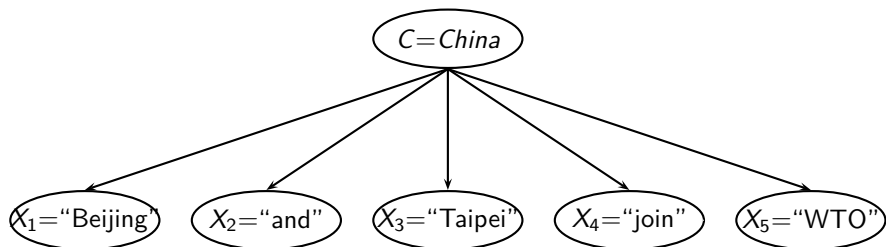


$$P(\text{China}|d) \propto P(\text{China}) \cdot P(\text{"Beijing"}|\text{China}) \cdot P(\text{"and"}|\text{China}) \\ \cdot P(\text{"Taipei"}|\text{China}) \cdot P(\text{"join"}|\text{China}) \cdot P(\text{"WTO"}|\text{China})$$

- If "WTO" never occurs in class China in the train set:

$$\hat{P}(\text{"WTO"}|\text{China}) = \frac{T_{\text{China}, \text{"WTO"}}}{\sum_{t' \in V} T_{\text{China}, t'}} = \frac{0}{\sum_{t' \in V} T_{\text{China}, t'}} = 0$$

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- → We will get $P(\text{China} | d) = 0$ for any document that contains WTO!

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- Now: Add one to each count to avoid zeros:

$$\hat{P}(t|c) = \frac{T_{ct} + 1}{\sum_{t' \in V} (T_{ct'} + 1)} = \frac{T_{ct} + 1}{(\sum_{t' \in V} T_{ct'}) + B}$$

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- For a new document, for each class, compute sum of (i) log of prior and (ii) logs of conditional probabilities of the terms
- Assign the document to the class with the largest score

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TRAINMULTINOMIALNB(\mathbb{C}, \mathbb{D})

```
1   $V \leftarrow \text{EXTRACTVOCABULARY}(\mathbb{D})$ 
2   $N \leftarrow \text{COUNTDOCS}(\mathbb{D})$ 
3  for each  $c \in \mathbb{C}$ 
4  do  $N_c \leftarrow \text{COUNTDOCSINCLASS}(\mathbb{D}, c)$ 
5      $prior[c] \leftarrow N_c/N$ 
6      $text_c \leftarrow \text{CONCATENATETEXTOFALLDOCSINCLASS}(\mathbb{D}, c)$ 
7     for each  $t \in V$ 
8     do  $T_{ct} \leftarrow \text{COUNTTOKENSOFTERM}(text_c, t)$ 
9     for each  $t \in V$ 
10    do  $condprob[t][c] \leftarrow \frac{T_{ct}+1}{\sum_{t'}(T_{ct'}+1)}$ 
11  return  $V, prior, condprob$ 
```

Naive Bayes: Testing

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```
APPLYMULTINOMIALNB( $\mathbb{C}$ ,  $V$ ,  $prior$ ,  $condprob$ ,  $d$ )  
1  $W \leftarrow \text{EXTRACTTOKENSFROMDOC}(V, d)$   
2 for each  $c \in \mathbb{C}$   
3 do  $score[c] \leftarrow \log prior[c]$   
4   for each  $t \in W$   
5     do  $score[c] + = \log condprob[t][c]$   
6 return  $\text{argmax}_{c \in \mathbb{C}} score[c]$ 
```

Exercise: Estimate parameters, classify test set

	docID	words in document	in $c = \textit{China}$?
training set	1	Chinese Beijing Chinese	yes
	2	Chinese Chinese Shanghai	yes
	3	Chinese Macao	yes
	4	Tokyo Japan Chinese	no
test set	5	Chinese Chinese Chinese Tokyo Japan	?

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$$\hat{P}(t|c) = \frac{T_{ct} + 1}{\sum_{t' \in V} (T_{ct'} + 1)} = \frac{T_{ct} + 1}{(\sum_{t' \in V} T_{ct'}) + B}$$

(B is the number of bins – in this case the number of different words or the size of the vocabulary $|V| = M$)

$$c_{\text{map}} = \operatorname{argmax}_{c \in C} [\hat{P}(c) \cdot \prod_{1 \leq k \leq n_d} \hat{P}(t_k|c)]$$

Example: Parameter estimates

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Priors: $\hat{P}(c) = 3/4$ and $\hat{P}(\bar{c}) = 1/4$

Conditional probabilities:

$$\hat{P}(\text{"Chinese"}|c) = (5 + 1)/(8 + 6) = 6/14 = 3/7$$

$$\hat{P}(\text{"Tokyo"}|c) = \hat{P}(\text{"Japan"}|c) = (0 + 1)/(8 + 6) = 1/14$$

$$\hat{P}(\text{"Chinese"}|\bar{c}) = (1 + 1)/(3 + 6) = 2/9$$

$$\hat{P}(\text{"Tokyo"}|\bar{c}) = \hat{P}(\text{"Japan"}|\bar{c}) = (1 + 1)/(3 + 6) = 2/9$$

The denominators are $(8 + 6)$ and $(3 + 6)$ because the lengths of $text_c$ and $text_{\bar{c}}$ are 8 and 3, respectively, and because the constant B is 6 as the vocabulary consists of six terms.

Example: Classification

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$$\hat{P}(c|d_5) \propto 3/4 \cdot (3/7)^3 \cdot 1/14 \cdot 1/14 \approx 0.0003$$

$$\hat{P}(\bar{c}|d_5) \propto 1/4 \cdot (2/9)^3 \cdot 2/9 \cdot 2/9 \approx 0.0001$$

Thus, the classifier assigns the test document to $c = \textit{China}$. The reason for this classification decision is that the three occurrences of the positive indicator “Chinese” in d_5 outweigh the occurrences of the two negative indicators “Japan” and “Tokyo”.

UNK

An UNK is a word that occurs in the test set, but did not occur in the training set.

- Option 1: Simply ignore UNKs
- Option 2: Add UNK to the training vocabulary
 - All counts $T_{c\text{UNK}}$ are zero (since UNK does not occur in training set).
 - All words in the test set that did not occur in the training set are replaced by “UNK”.

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- 4 Evaluation of TC

Naive Bayes: Analysis

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- We will formally derive the classification rule ...
- ...and make our assumptions explicit.

Derivation of Naive Bayes rule

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We want to find the class that is most likely given the document:

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} P(c|d)$$

Apply Bayes rule $P(A|B) = \frac{P(B|A)P(A)}{P(B)}$:

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} \frac{P(d|c)P(c)}{P(d)}$$

Drop denominator since $P(d)$ is the same for all classes:

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} P(d|c)P(c)$$

Too many parameters / sparseness

$$\begin{aligned}c_{\text{map}} &= \operatorname{argmax}_{c \in \mathbb{C}} P(d|c)P(c) \\ &= \operatorname{argmax}_{c \in \mathbb{C}} P(\langle t_1, \dots, t_k, \dots, t_{n_d} \rangle | c)P(c)\end{aligned}$$

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- We would need a very, very large number of training examples to estimate that many parameters.
- This is the problem of **data sparseness**.

Bag of words model

To reduce the number of parameters to a manageable size, we make the **Naive Bayes conditional independence (bedingte Unabhängigkeit)** assumption:

$$P(d|c) = P(\langle t_1, \dots, t_{n_d} \rangle | c) = \prod_{1 \leq k \leq n_d} P(X_k = t_k | c)$$

We assume that the probability of observing the conjunction of attributes is equal to the product of the individual probabilities $P(X_k = t_k | c)$.

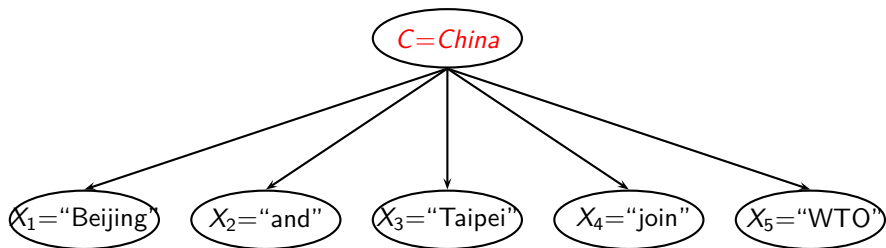
Recall from earlier the estimates for these conditional probabilities:

$$\hat{P}(t|c) = \frac{T_{ct} + 1}{(\sum_{t' \in V} T_{ct'}) + B}$$

This can be referred to as a **bag of words model**.

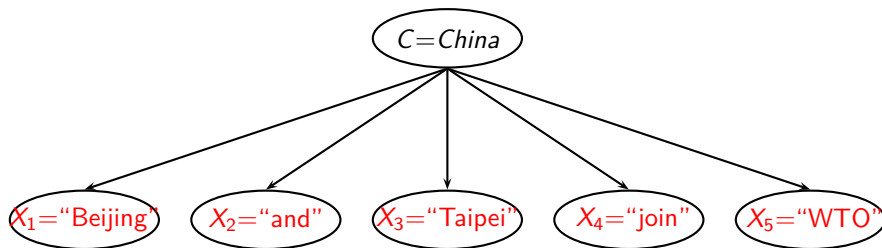
Generative model

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$$P(c|d) \propto P(c) \prod_{1 \leq k \leq n_d} P(t_k|c)$$

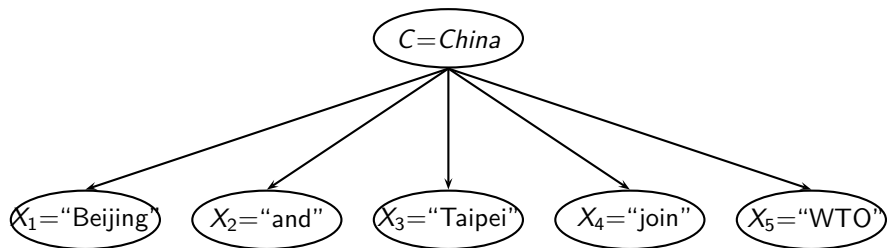
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- Generate a class with probability $P(c)$
- Generate each of the words (in their respective positions), conditional on the class, but independent of each other, with probability $P(t_k|c)$
- To classify docs, we “reengineer” this process and find the class that is most likely to have generated the doc.

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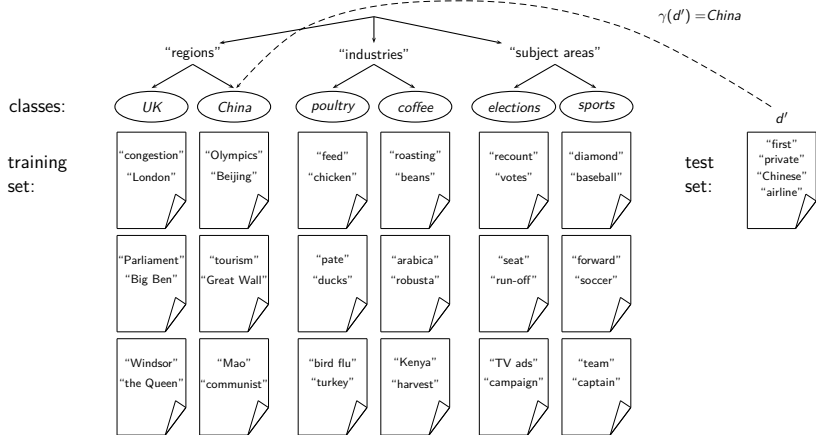
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- Low storage requirements

Outline

- 1 Text classification
- 2 Naive Bayes
- 3 NB theory
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Evaluation on Reuters



Example: The Reuters collection

symbol	statistic	value
N	documents	800,000
L	avg. # word tokens per document	200
M	word types	400,000

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type of class	number	examples
region	366	UK, China
industry	870	poultry, coffee
subject area	126	elections, sports

A Reuters document



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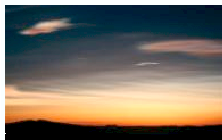
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Extreme conditions create rare Antarctic clouds

Tue Aug 1, 2006 3:20am ET

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SYDNEY (Reuters) - Rare, mother-of-pearl colored clouds caused by extreme weather conditions above Antarctica are a possible indication of global warming, Australian scientists said on Tuesday.

Known as nacreous clouds, the spectacular formations showing delicate wisps of colors were photographed in the sky over an Australian

Evaluating classification

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- Evaluation must be done on test data that are independent of the training data, i.e., training and test sets are disjoint.
- It's easy to get good performance on a test set that was available to the learner during training (e.g., just memorize the test set).
- Measures: Precision, recall, F_1 , classification accuracy

Precision P and recall R

	in the class	not in the class
predicted to be in the class	true positives (TP)	false positives (FP)
predicted to not be in the class	false negatives (FN)	true negatives (TN)

TP, FP, FN, TN are counts of documents. The sum of these four counts is the total number of documents.

$$\text{precision: } P = TP / (TP + FP)$$

$$\text{recall: } R = TP / (TP + FN)$$

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- In most application scenarios, we need both good precision and good recall.
- So we need to find a good **precision-recall** tradeoff.

A combined measure: F_1

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- The harmonic mean is a kind of “soft” minimum.

$$\text{accuracy} = \frac{\text{TP} + \text{TN}}{\text{TP} + \text{TN} + \text{FP} + \text{FN}}$$

F_1 scores for Naive Bayes vs. other methods

(a)	NB	Rocchio	kNN	SVM	
micro-avg-L (90 classes)	80	85	86	89	
macro-avg (90 classes)	47	59	60	60	

(b)	NB	Rocchio	kNN	trees	SVM
earn	96	93	97	98	98
acq	88	65	92	90	94
money-fx	57	47	78	66	75
grain	79	68	82	85	95
crude	80	70	86	85	89
trade	64	65	77	73	76
interest	65	63	74	67	78
ship	85	49	79	74	86
wheat	70	69	77	93	92
corn	65	48	78	92	90
micro-avg (top 10)	82	65	82	88	92
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Naive Bayes does pretty well, but some methods beat it consistently (e.g., SVM).

Confusion matrix for Reuters-21578

	assigned class:	<i>money-fx</i>	<i>trade</i>	<i>interest</i>	<i>wheat</i>	<i>corn</i>	<i>grain</i>
true class:							
<i>money-fx</i>		95	0	10	0	0	0
<i>trade</i>		1	1	90	0	1	0
<i>interest</i>		13	0	0	0	0	0
<i>wheat</i>		0	0	1	34	3	7
<i>corn</i>		1	0	2	13	26	5
<i>grain</i>		0	0	2	14	5	10

Example: 14 documents from *grain* were incorrectly assigned to *wheat*.

Exercise

Compute precision, recall and F_1 :

	in class	not in class
predicted to be in class	TP: 18	FP: 2
predicted not to be in class	FN: 82	TN: 1,000,000,000

$$\text{precision: } P = TP / (TP + FP)$$

$$\text{recall: } R = TP / (TP + FN)$$

$$F_1 = \frac{2PR}{P + R}$$

- What is text classification?
(or: What is sentence classification?)
- Naive Bayes classification rule
- Estimation of Naive Bayes priors and conditionals
- Theory: Bag of words model
 - Maximum likelihood
 - Add-one = Laplace
- Precision, recall, F_1
- Precision-recall tradeoff
- Confusion matrix